

**Warming caused by cumulative carbon  
emissions: the trillionth tonne**  
PRIMA Congress, Sydney, July, 2009

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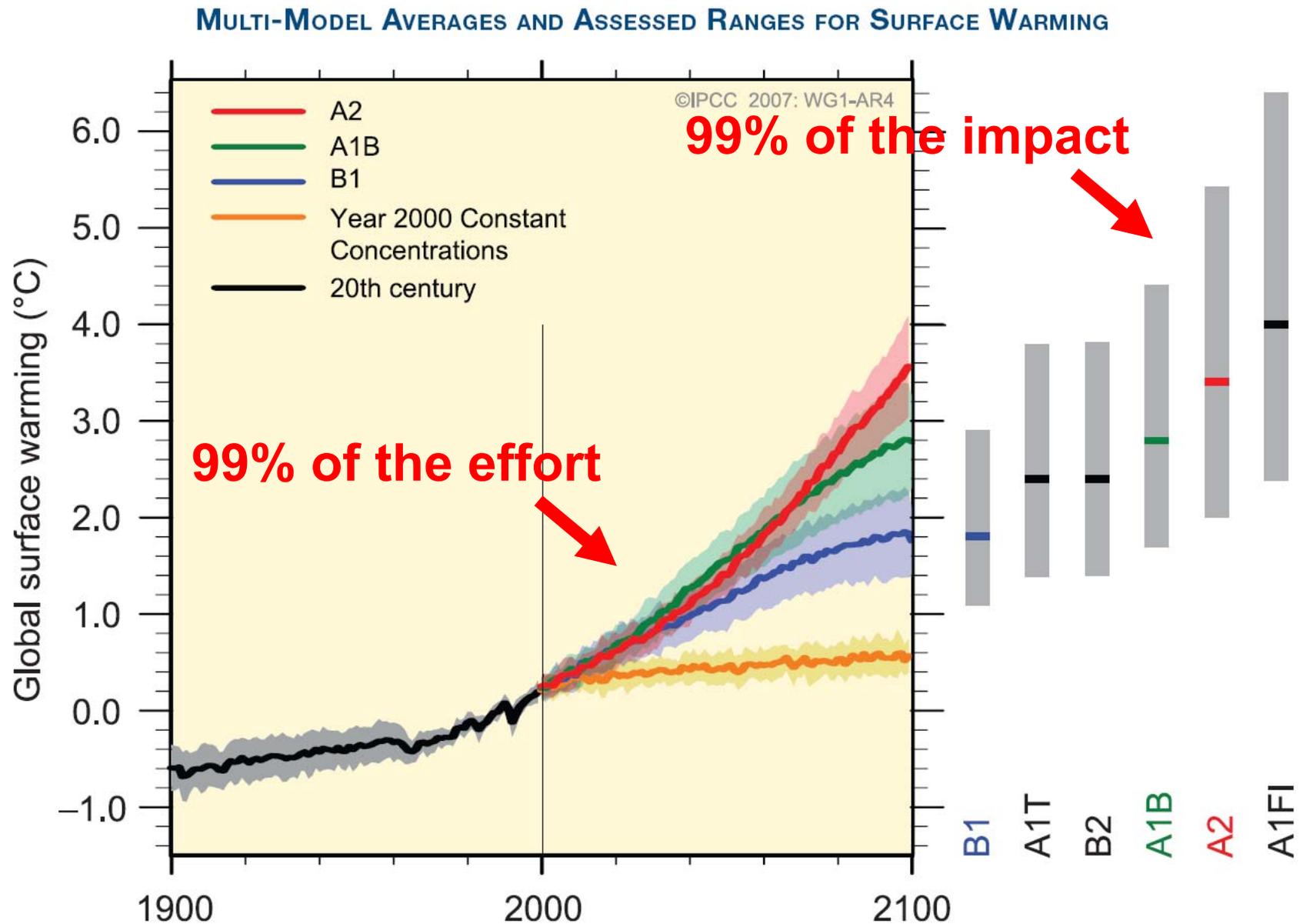


# Sources of uncertainty in climate forecasting

- **Initial condition uncertainty:**
  - Technically irrelevant to *climate* forecasts, but important because distinction between internal state and boundary conditions is fuzzy: is the Greenland ice cap part of the weather, or a boundary condition on the climate?
- **Boundary condition uncertainty:**
  - Natural (solar and volcanic) forcing: poorly known, but conceptually straightforward.
  - Anthropogenic (mostly greenhouse gas emissions): all muddled up in politics, but Somebody Else's Problem.
- **Response uncertainty, or “model error”:**
  - The subject of this lecture.



# A recent failure of climate modelling



# What is the aim of climate modeling?

- **Recent Reading conference called for \$1bn “revolution in climate modeling”.**
- **How do we know when the revolution is over?**
  - When we have a 25km resolution global climate model.
  - When we have a 1km resolution global climate model.
  - When we don’t need to parameterize clouds.
  - When we have a bigger computer than the weapons developers.
- **Or:**
  - When, no matter how we perturb our climate models, the distribution of future climates consistent with observations of past and current climate is the same.



# The conventional Bayesian approach to probabilistic climate forecasting

$$P(S | y) = \int_{\theta} P(S | \theta) P(\theta | y) d\theta$$
$$= \int_{\theta} P(S | \theta) \frac{P(y | \theta) P(\theta)}{P(y)} d\theta$$

$S$  quantity predicted by the model, e.g. “climate sensitivity”

$\theta$  model parameters, e.g. diffusivity, entrainment coefficient etc.

$y$  observations of model-simulated quantities e.g. recent warming

$P(y|\theta)$  likelihood of observations  $y$  given parameters  $\theta$

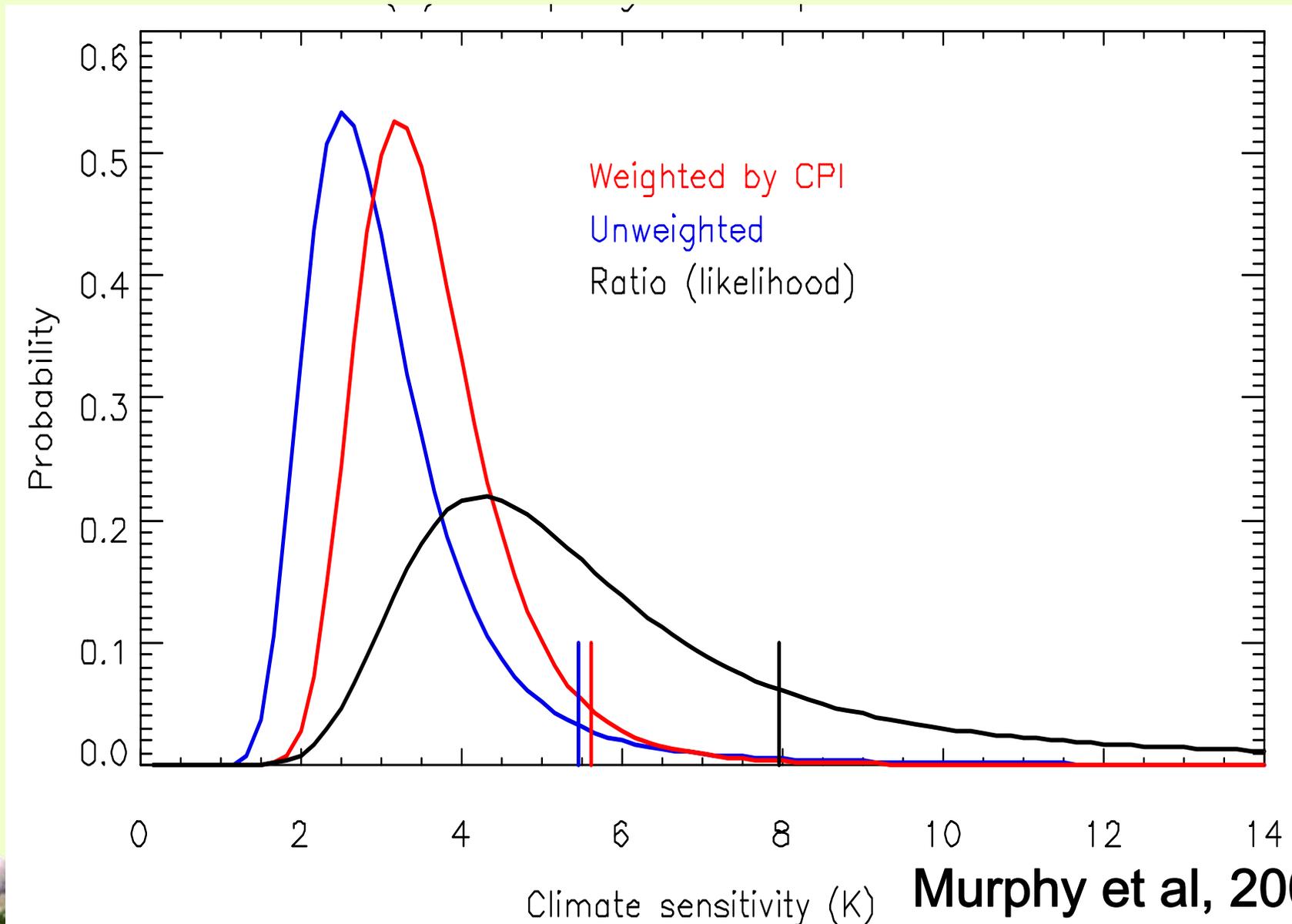
$P(\theta)$  prior distribution of parameters  $\theta$

Simple models:  $P(S|\theta)=1$  if parameters  $\theta$  gives sensitivity  $S$

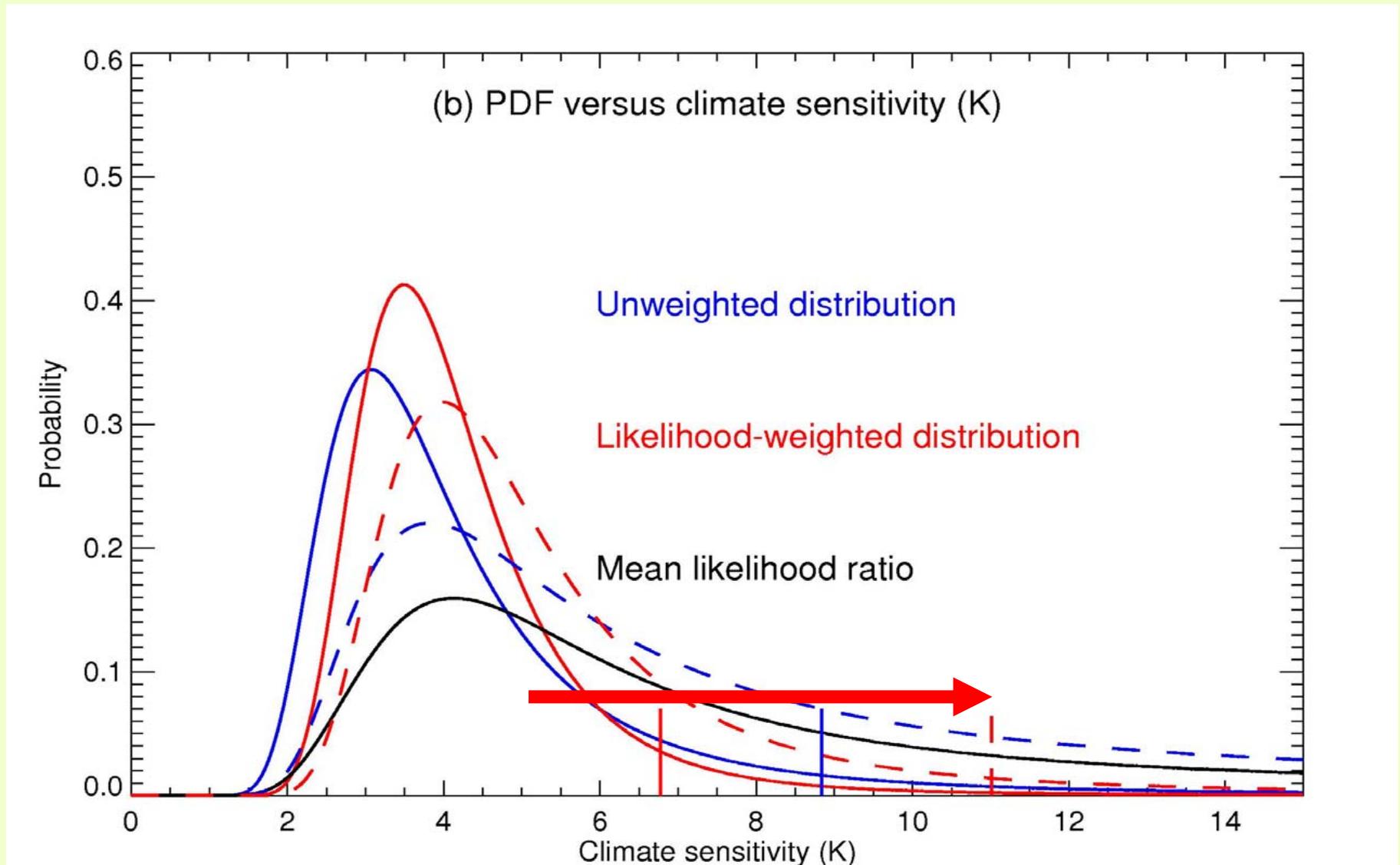
$P(S|\theta)=0$  otherwise



# Bayesian approach: sample parameters, run ensemble, “emulate” & weight by fit to observations



# Adopting alternative plausible parameter sampling designs has a big impact on results



# Why the standard Bayesian approach won't ever work

- Sampling a distribution of “possible models” requires us to define a distance between two models in terms of their input parameters & structure, a “metric for model error”.
- As long as models contain “nuisance parameters” that do not correspond to any observable quantity, this is impossible in principle: definition of these parameters in the model is arbitrary.



# Why we need a different approach

- There's no such thing as a neutral or uninformative prior in this problem.
- Very difficult to avoid impression that investigators are subject to external pressures to adopt the “right” prior (the one that gives the answer people want).
- Highly informative priors obscure the role of new observations, making it very difficult to make “progress” (the 1.5-4.5K problem).
- So what is the alternative?



# A more robust approach: compute *maximum likelihood* over all models that predict a given $S$

$$L_1(S | y) = \max_{\theta} P(S | \theta) P(y | \theta)$$

$P(S|\theta)$  picks out models that predict a given value of the forecast quantity of interest, e.g. climate sensitivity.

$P(y|\theta)$  evaluates their likelihoods.

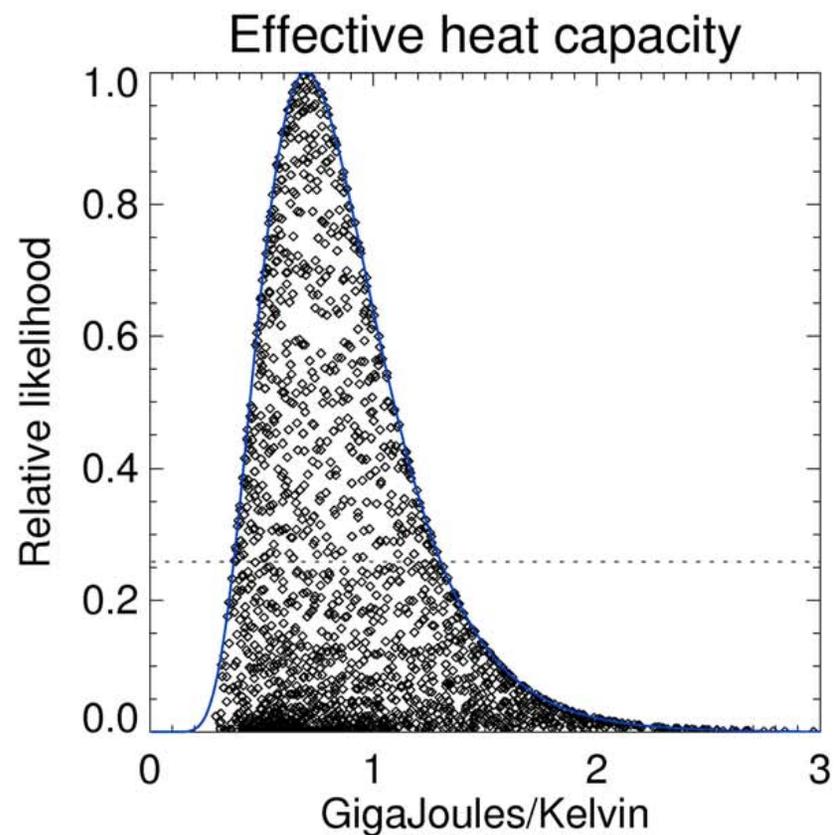
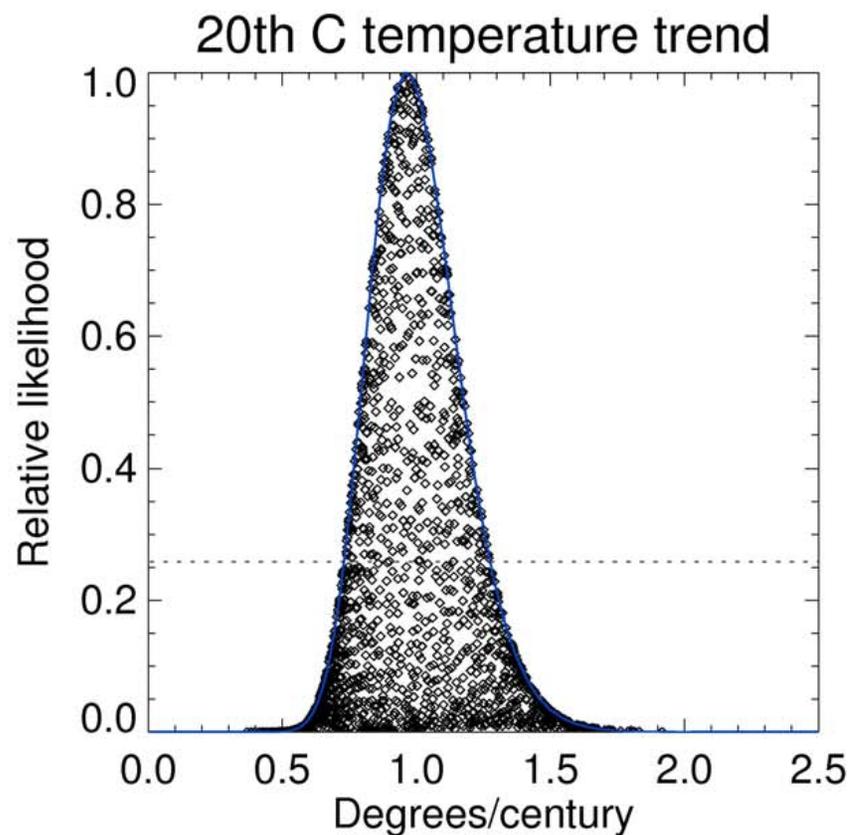
Likelihood profile,  $L_1(S|y)$ , is proportional to relative likelihood of most likely available model as a function of forecast quantity.

Likelihood profiles follow parameter combinations that cause likelihood to fall off as slowly as possible with  $S$ : the “least favourable sub-model” approach.

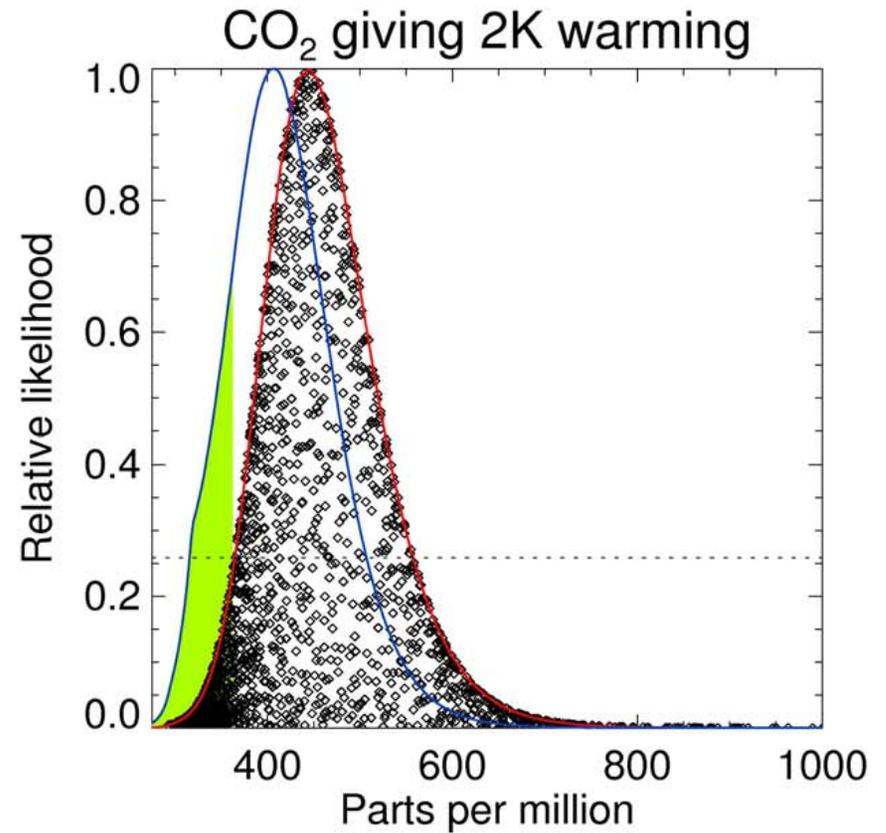
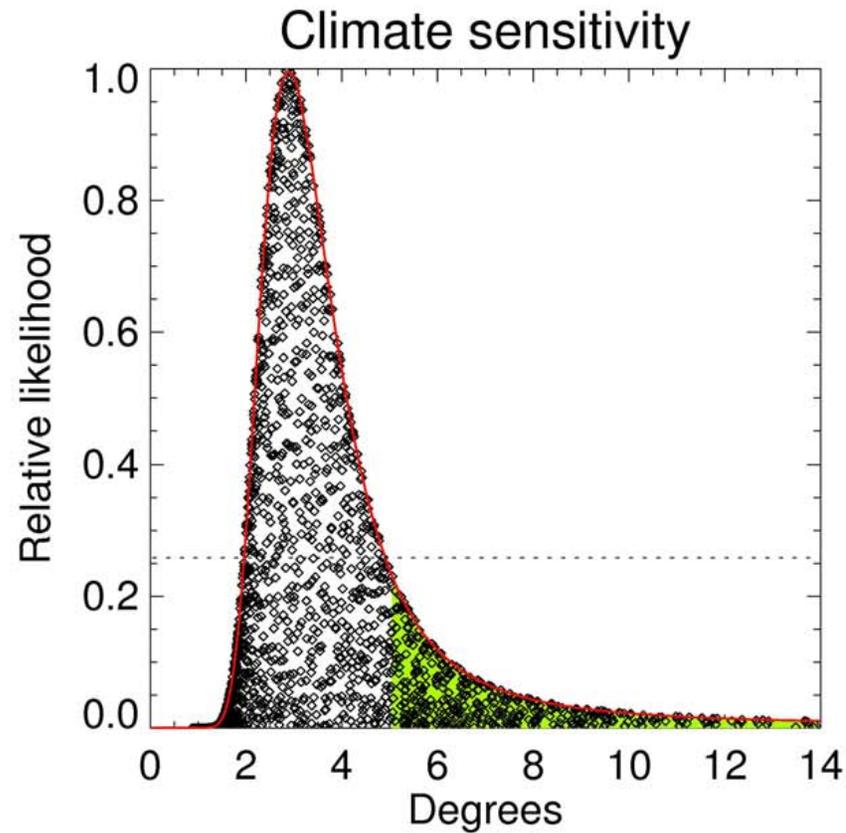
$P(\theta)$  does not matter. Use any sampling design you like as long as you find the likelihood maxima.



# Generating models consistent with quantities we can observe...



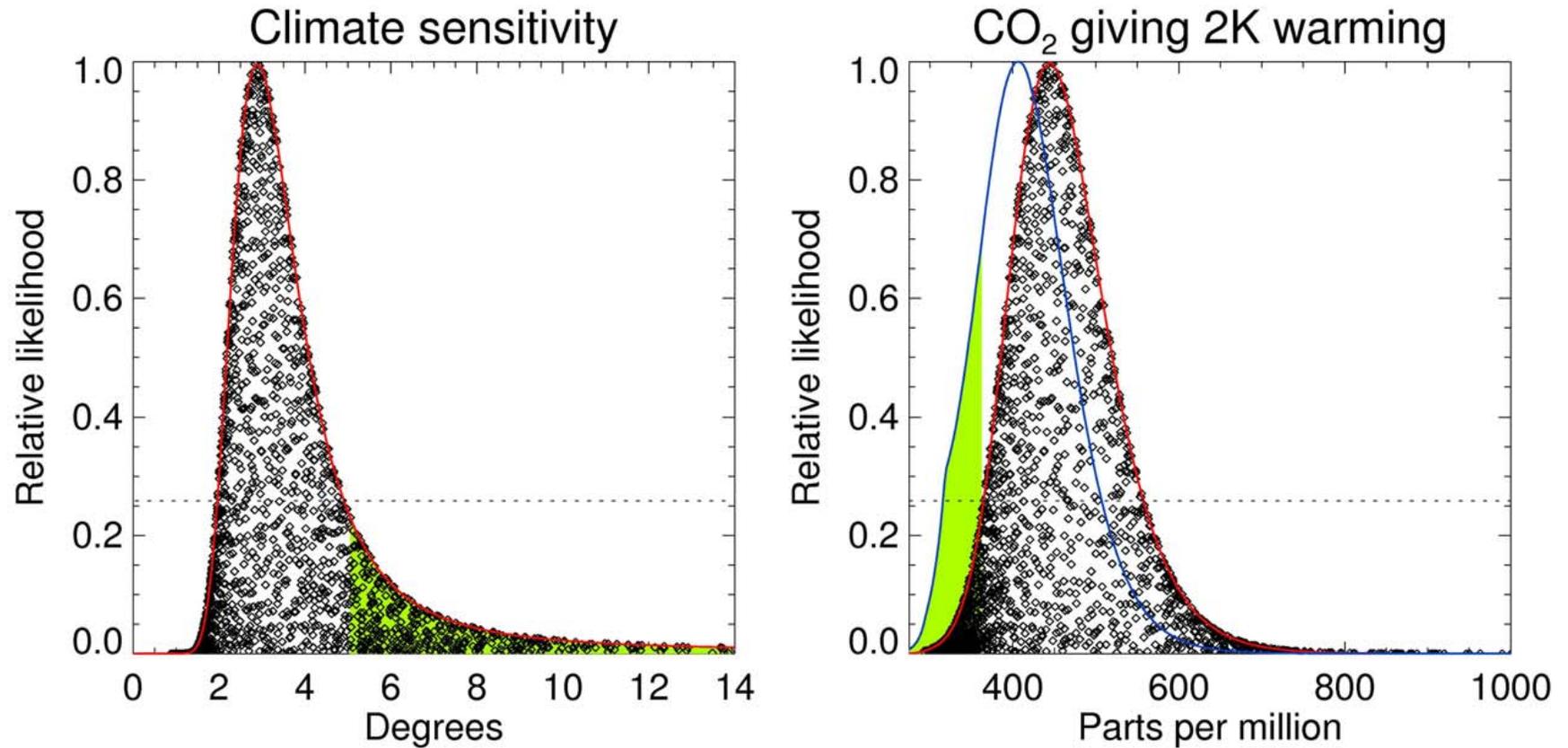
# ...and mapping their implications for quantities we wish to forecast.



**Note: only the outline (likelihood profile) matters, not the density of models. Hence we avoid the metric-of-model-error problem.**



# This gives confidence intervals, not PDFs



**Non-linear relationship between climate sensitivity and CO<sub>2</sub> concentrations giving 2K warming.**  
**Straightforward to generate conventional confidence intervals.**  
**Consistent posterior PDFs require a consistent, and one-way-or-the-other informative, prior.**



# The problem with equilibrium climate sensitivity...

- ...is that it is not related linearly to anything we can observe, so any forecast distribution is inevitably dependent on arbitrary choices of prior.
- Conventional policy of specifying stabilization targets appears to require a distribution of climate sensitivity.
- Is there an alternative way of approaching the long-term climate forecast which is less sensitive to these issues?



# What would it take to avoid dangerous levels of warming?



**Nature, April  
30<sup>th</sup> 2009**



[climateprediction.net](http://climateprediction.net)

Oxford University



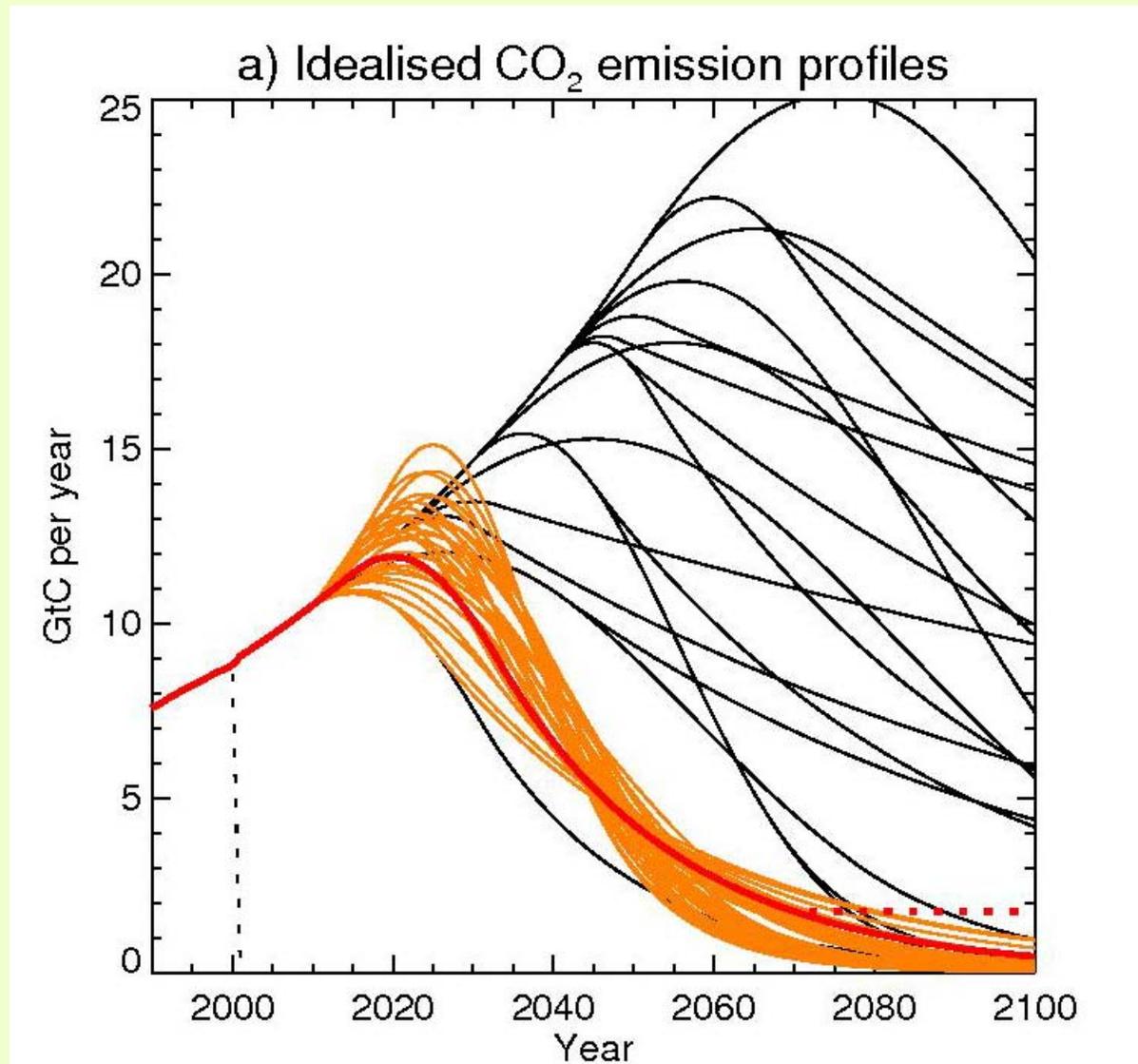
# Summary of the study

- **Generate idealised CO<sub>2</sub> emission scenarios varying:**
  - Initial rate of exponential growth from 2010 (1-3%/year).
  - Year in which growth begins to slow down (2012 to 2050).
  - Rate at which growth slows and reverses.
  - Maximum rate of emission decline (up to -10%/year).
  - Exponential decline continues indefinitely (or until temperatures peak).
- **Simulate response using simple coupled climate carbon-cycle models constrained by observations.**
- **Identify factors that determine “damage”, defined as:**
  - Peak warming over pre-industrial (relevant to ecosystems).
  - Average warming 2000-2500 (relevant to ice-sheets).
  - Warming by 2100 (relevant to IPCC).



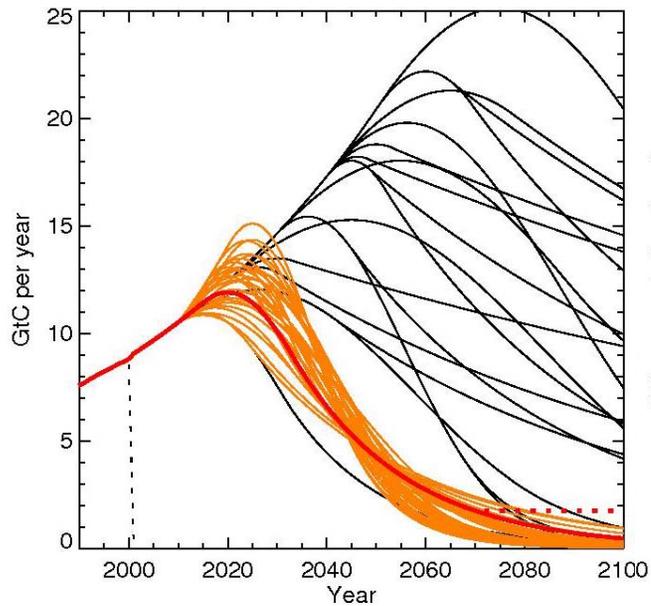


# Red and orange scenarios all have cumulative emissions of 1TtC (=1EgC=3.7TtCO<sub>2</sub>)

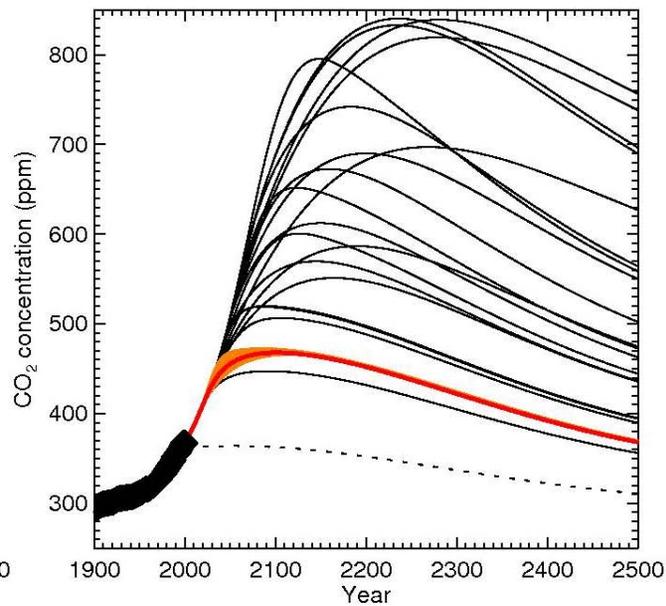


# Timing and size of emission peak does not *in itself* determine peak warming

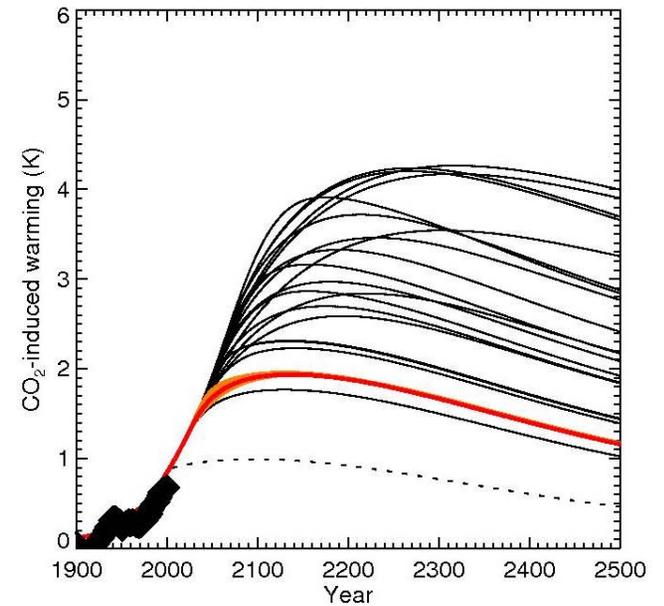
## Emissions



## CO<sub>2</sub> concentrations

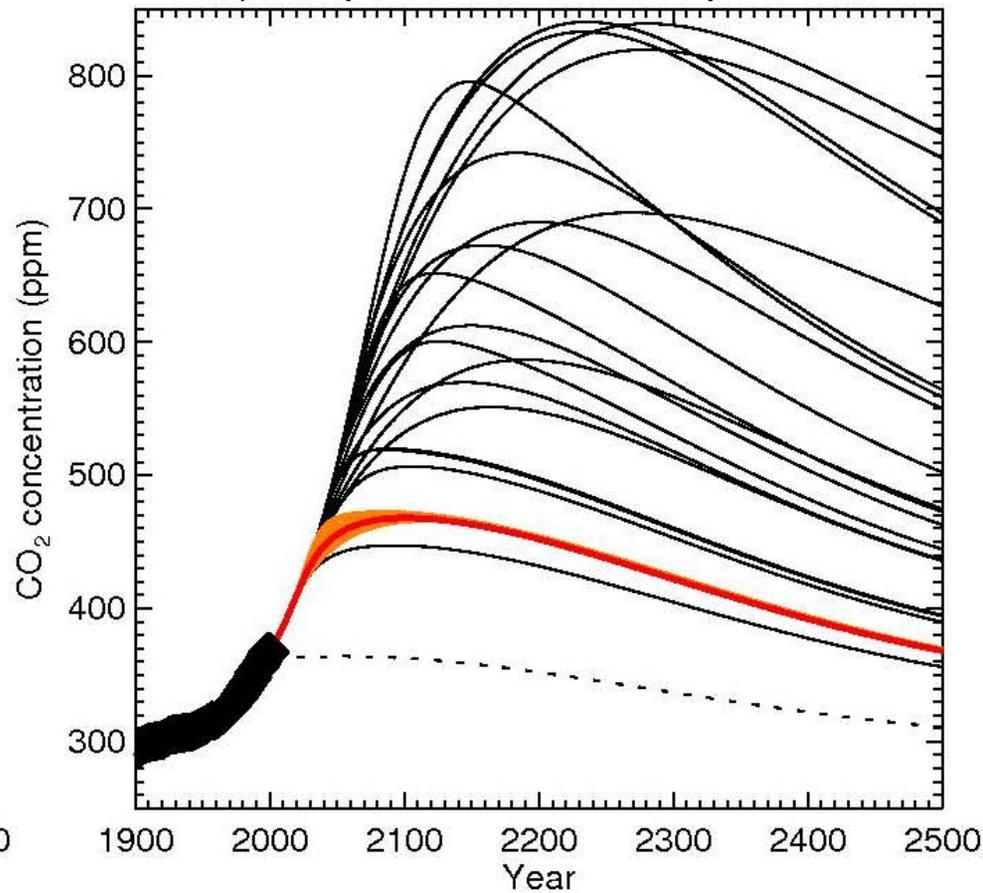


## CO<sub>2</sub>-induced warming

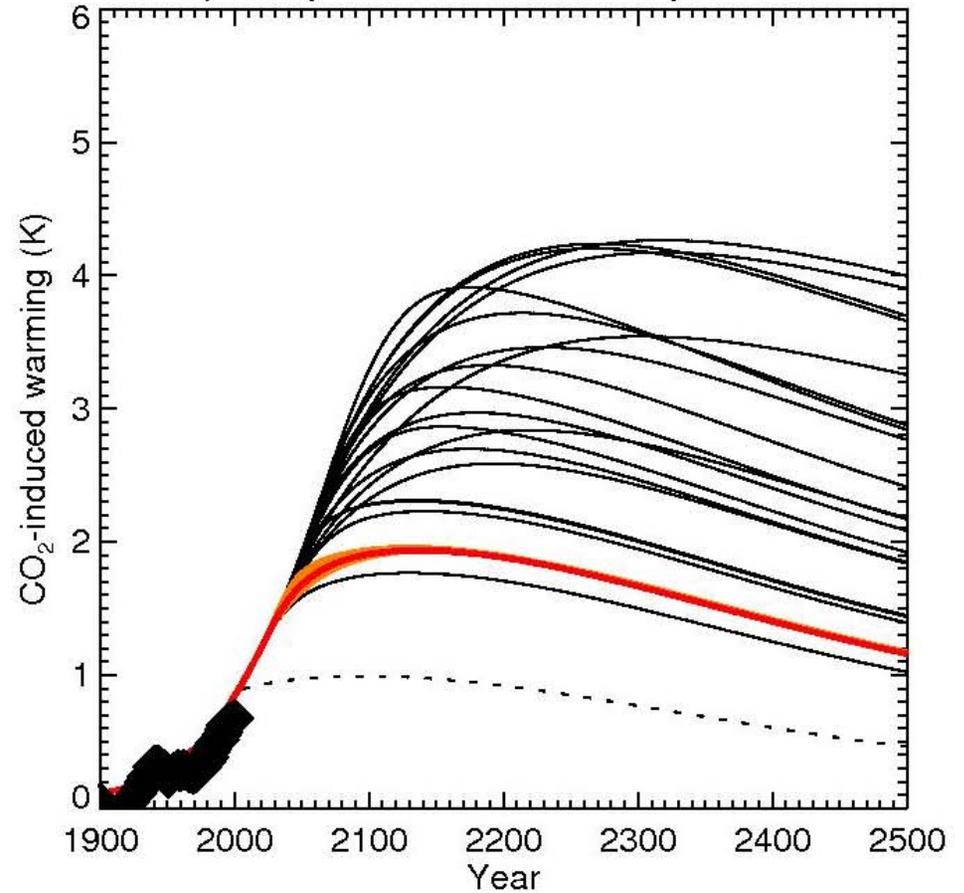


# Response with best-fit model parameters

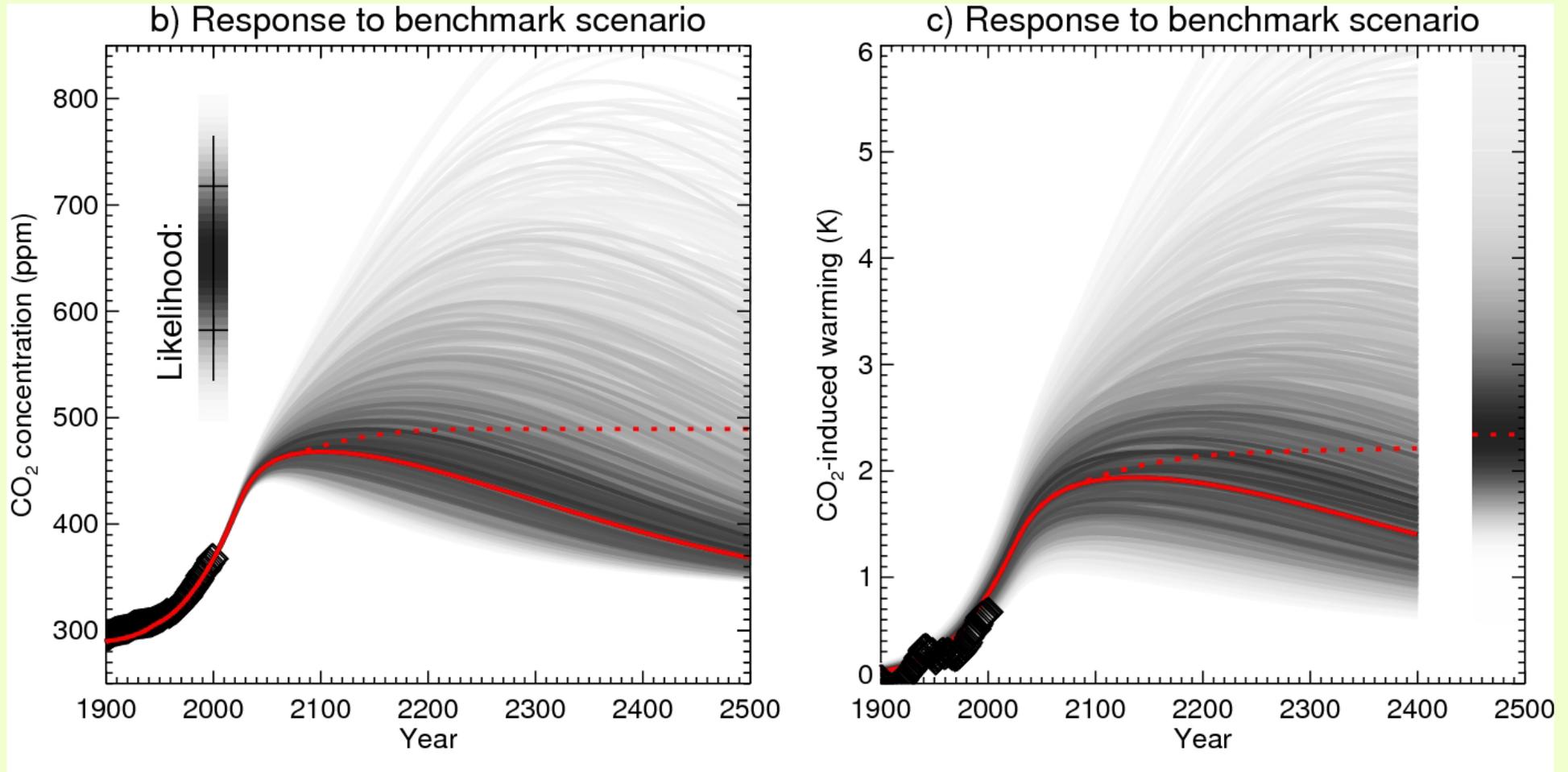
## CO<sub>2</sub> concentrations



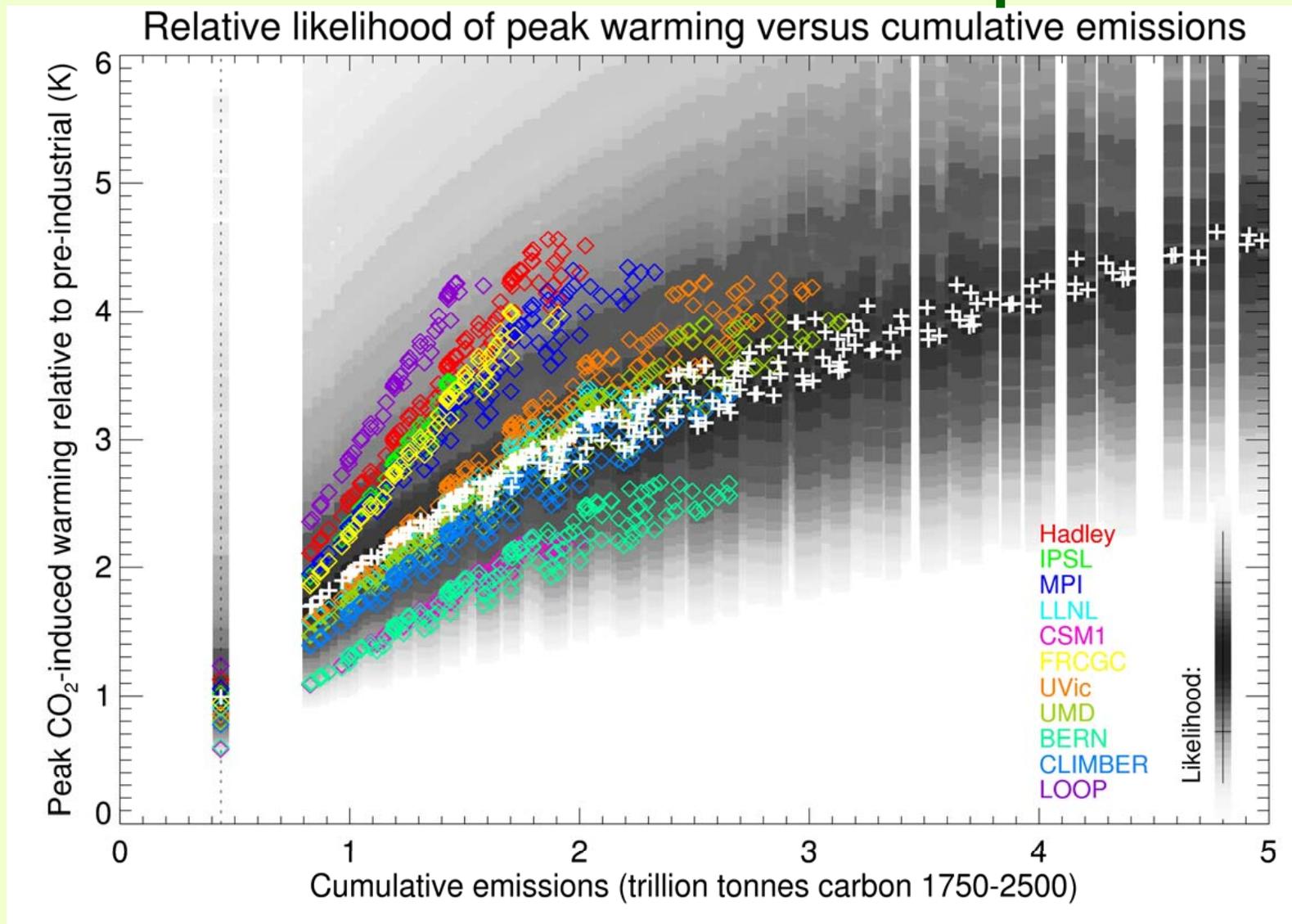
## CO<sub>2</sub>-induced warming



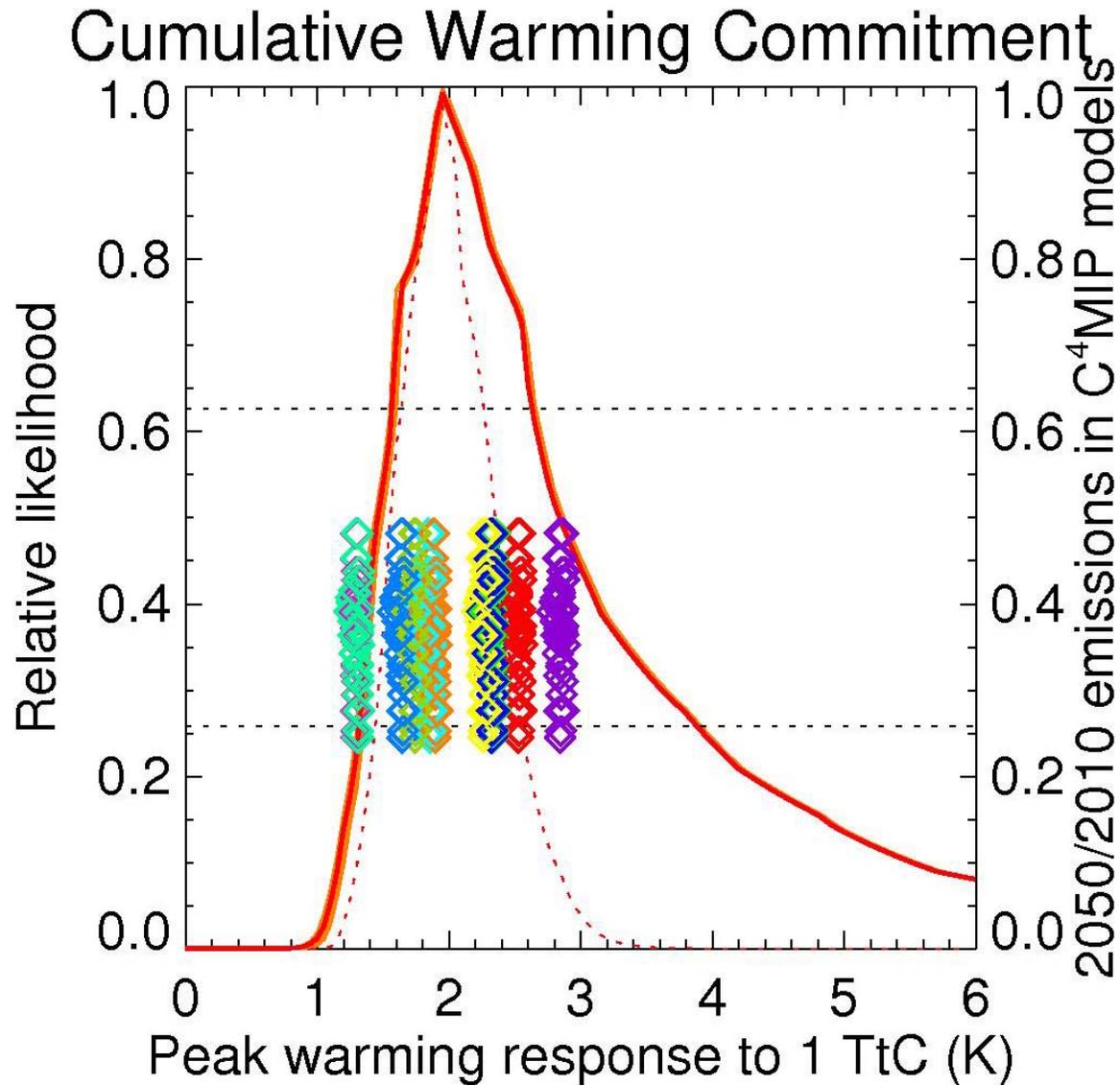
# Uncertainty in the response dwarfs the impact of timing of emissions or size of emission peak



# Peak warming is determined by total amount of carbon released into the atmosphere...

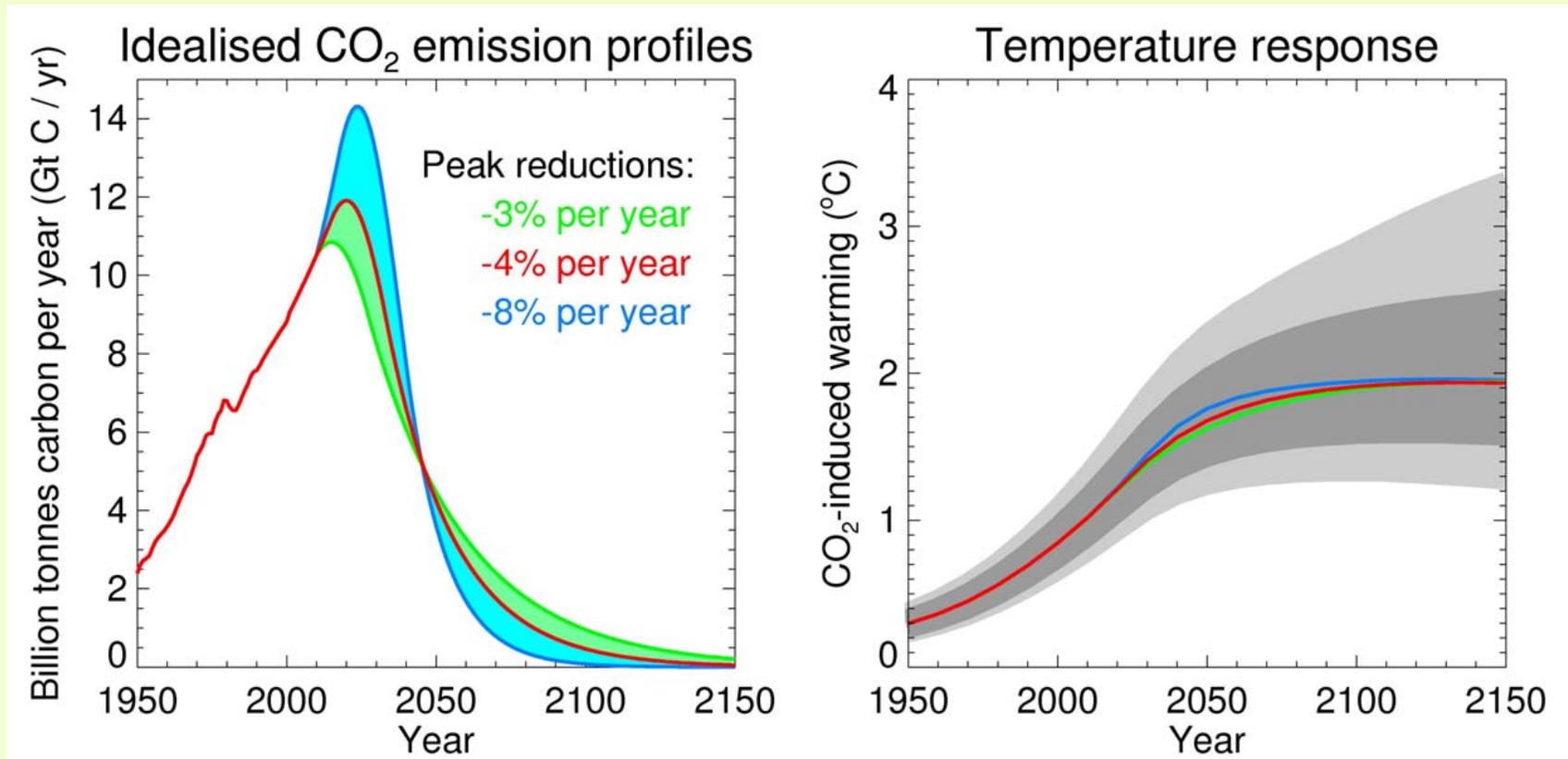


# ...not by emissions in 2050

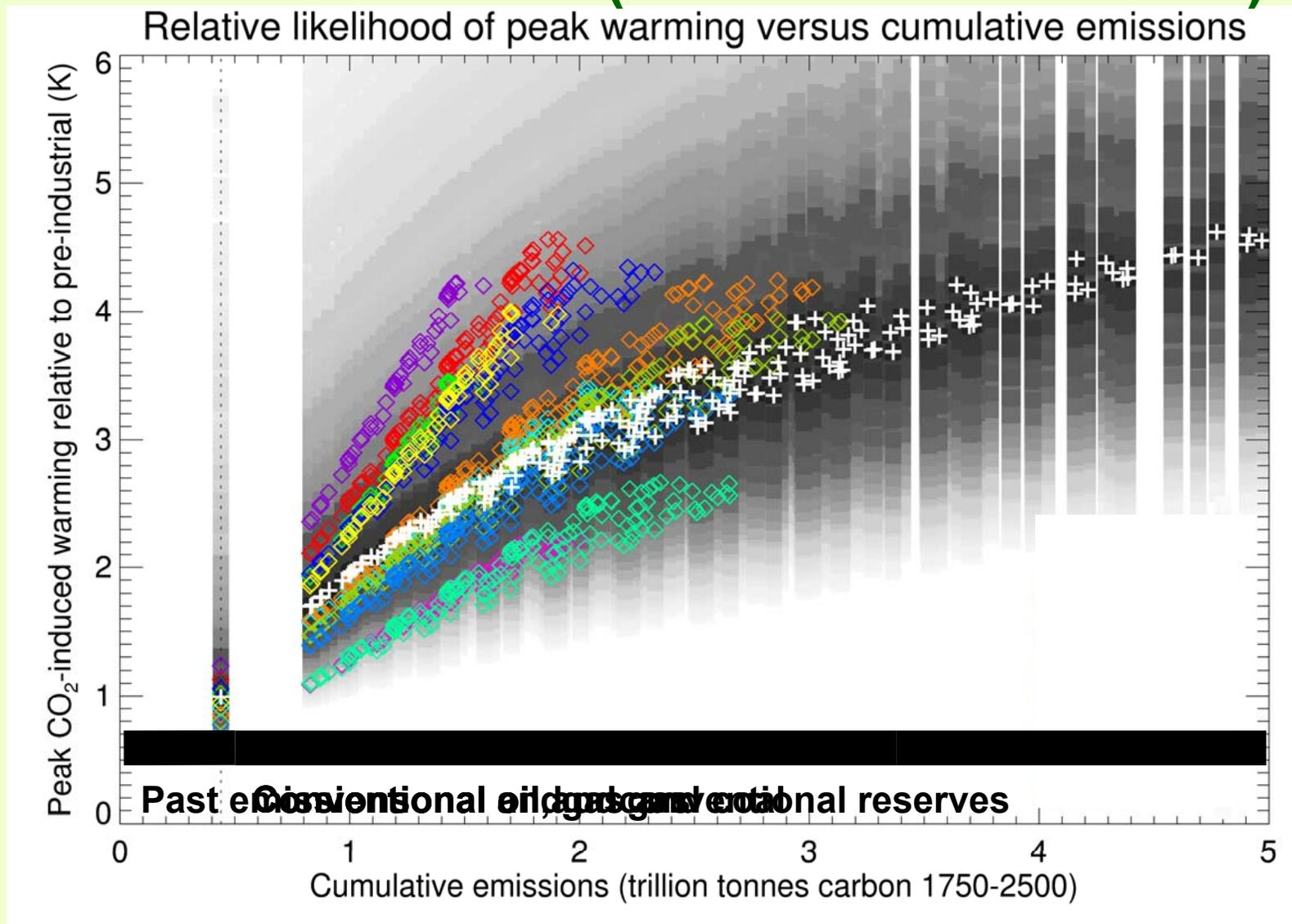


# Implications: are we debating the wrong thing?

- Warming caused by CO<sub>2</sub> depends on cumulative emissions, not emissions in 2020 or 2050.
- Releasing carbon slower makes little difference to climate (but a big difference to cost of mitigation).



# How cumulative emissions stack up against fossil fuel reserves (IPCC AR4 estimates)

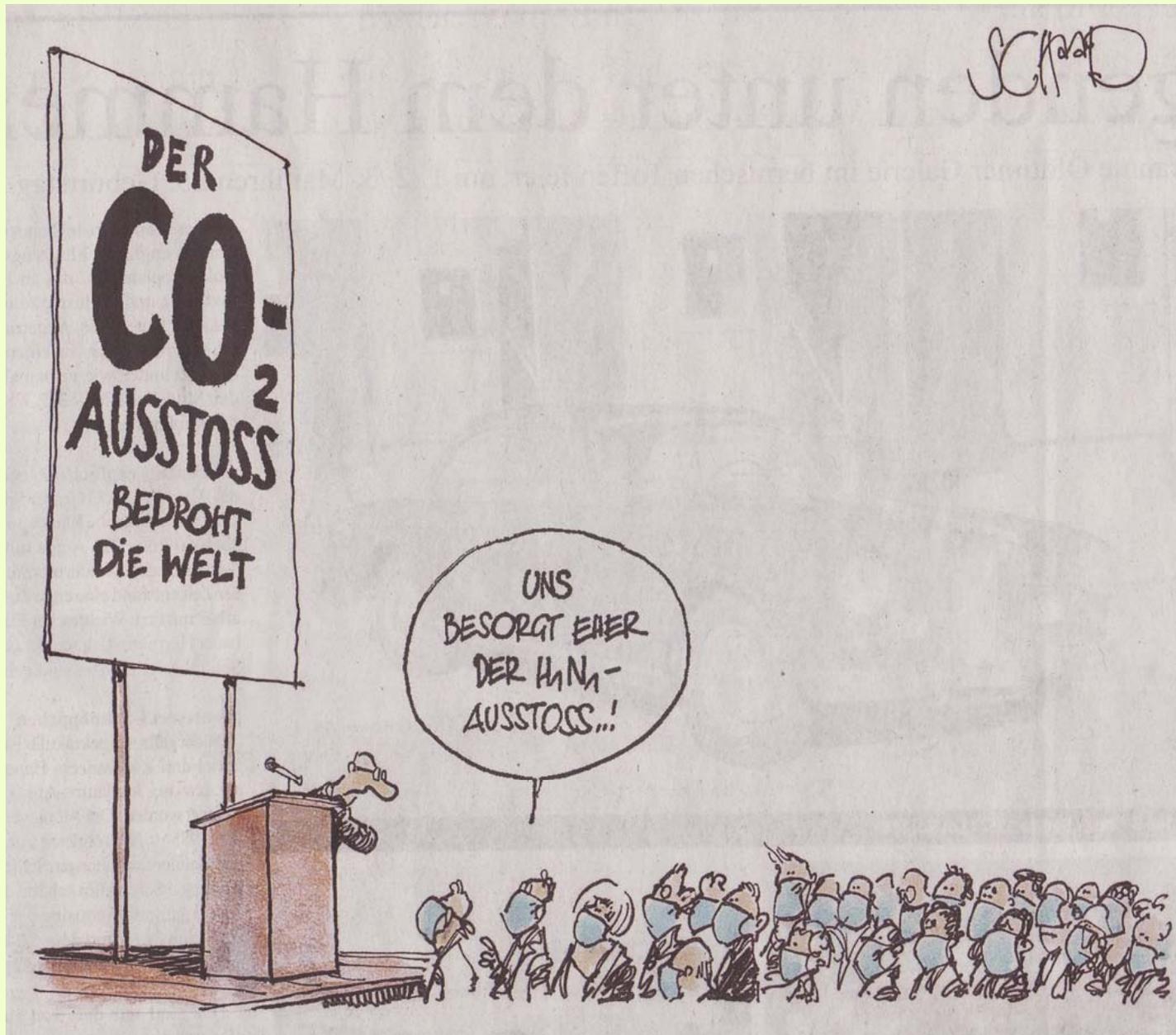


# Conclusions & links to other studies

- Cumulative CO<sub>2</sub> emissions over the entire anthropocene determine peak CO<sub>2</sub>-induced warming.
- Warming response to cumulative emissions is constrained by past CO<sub>2</sub> increase and CO<sub>2</sub>-induced warming. You do *not* need to know the:
  - Equilibrium climate sensitivity.
  - Long term target GHG stabilisation level.
  - Date and size of emission peak, or details of emission path (2000-2050 emissions determine total for most low scenarios).
- **1TtC** gives **most likely** CO<sub>2</sub>-induced warming of **2°C**.  
“Very likely” between **1.3-3.9°C**, “Likely” between **1.6-2.6°C**.  
M09: 1,440 GtCO<sub>2</sub><sub>(2000-2050)</sub> ≈ **0.9 TtC**<sub>(1750-2500)</sub> → **50% risk of >2°C**.  
M09: 1,000 GtCO<sub>2</sub><sub>(2000-2050)</sub> ≈ **0.71TtC**<sub>(1750-2500)</sub> → **25% risk of >2°C**.  
UKCCC: 2,500 GtCO<sub>2e</sub><sub>(1990-2050)</sub> ≈ **0.96TtC**<sub>(1750-2500)</sub> → **50% risk of >2°C**.



# Long-term targets in a short-term world



Felix Schaad,  
*Tagesanzeiger*,  
(Swiss national  
newspaper),  
April 30, 2009



# The model

- **Simple mixed-layer/diffusive energy balance model:**

$$a_1 \frac{dT}{dt} = a_3 \ln\left(\frac{C_1 + C_2 + C_3}{C_0}\right) - a_0 T - a_2 \int_0^t \frac{dT(t')}{dt'} \frac{dt'}{\sqrt{t-t'}}$$

- **“Revelle accumulation” of long-term equilibrium CO<sub>2</sub>:**

$$\frac{dC_3}{dt} = b_3 E$$

- **Slow advection of “active CO<sub>2</sub>” into deep ocean:**

$$\frac{dC_2}{dt} = b_1 E - b_0 C_2$$

- **Diffusive uptake by mixed layer and biosphere:**

$$\frac{dC_1}{dt} = b_4 E - b_2 \int_0^t \frac{dC_1(t')}{dt'} \frac{dt'}{\sqrt{t-t'}}$$

- **C-T feedback linear in ΔT above preceding century:**

$$E = E_a + b_5 T'$$

- **Emissions scaled to give correct 1960-2000 CO<sub>2</sub>.**



# The constraints

- Warming attributable to greenhouse gases over the 20<sup>th</sup> century.
- Effective ocean-troposphere-land heat capacity over 1959-98.
- CO<sub>2</sub> airborne fraction over 1960-2000 (uncertain due to uncertainty in land-use emissions).
- Contribution of C-T feedback to 2100 airborne fraction under A2 scenario (constrain with C4MIP).
- Rate of advection of active CO<sub>2</sub> into deep ocean (constrain with available EMICs).



# Constraints on Cumulative Warming Commitment

Climate system property, $X$	Most likely value of $X$	5-95% confidence interval	Reduction in fractional uncertainty in CWC due to reducing fractional uncertainty $\sigma_{\log(X)}$ by	
			0.05	50%
20 <sup>th</sup> century warming trend attributable to GHGs	0.97 °C/century	0.73-1.27 °C/century	18%	29%
Effective heat capacity 1955-98	0.70 GJ/°C	0.38-1.30 GJ/°C	1%	3%
Net airborne fraction (AF) 1960-2000	0.43	0.39-0.47	5%	0%
Contribution of temp. feedback to net AF 1766-2100	0.17	0.07-0.39	5%	13%
Rate constant for advection of CO <sub>2</sub> into deep ocean	200 years	133-302 years	0%	0%

